

5.4-5.6 Quiz Review

Name: Key

1. If $0^\circ \leq x \leq 360^\circ$, solve: $\csc x = -2$.

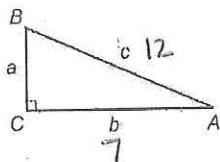
$$\sin x = -\frac{1}{2}$$

$$x = \boxed{210^\circ, 330^\circ}$$

2. Assuming an angle in Quadrant I, evaluate $\tan(\sec^{-1} \frac{13}{5})$.

$$\frac{13}{5} \quad \tan(\sec^{-1} \frac{13}{5}) = \boxed{\frac{12}{5}}$$

3. Given right triangle ABC, find B to the nearest tenth of a degree if $b = 7$ and $c = 12$.



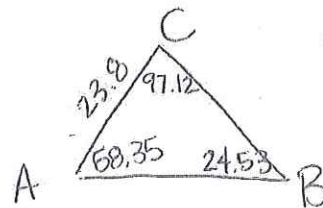
$$\sin B = \frac{7}{12}$$

$$B = \boxed{35.7^\circ}$$

Find each value. Round to the nearest tenth.

4. In $\triangle ABC$, $A = 58^\circ 21'$, $C = 97^\circ 07'$, and $b = 23.8$. Find a .

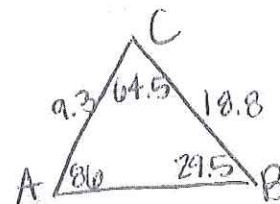
$$\frac{58.35}{100} \quad \frac{97.12}{100} \quad a \approx \boxed{48.8}$$



$$\frac{\sin 24.53}{23.8} = \frac{\sin 58.35}{a}$$

5. If $B = 29.5^\circ$, $C = 64.5^\circ$, and $a = 18.8$, find the area of $\triangle ABC$.

$$\frac{1}{2}(9.3)(18.8)\sin 64.5 \approx \boxed{78.7 \text{ in}^2}$$



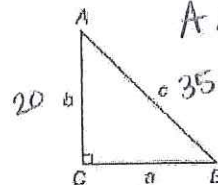
$$\frac{\sin 86}{18.8} = \frac{\sin 29.5}{b} \quad 9.3 \approx b$$

6. Solve $\triangle ABC$ given that $b = 20$ and $c = 35$.

$$\sin B = \frac{20}{35}$$

$$B = \sin^{-1} \frac{20}{35}$$

$$A = \boxed{55.2^\circ}$$



$$20^2 + a^2 = 35^2$$

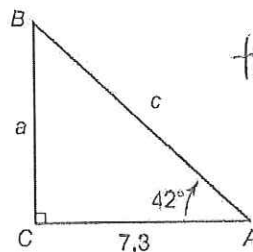
$$a \approx \boxed{28.7}$$

$$B = \boxed{34.8^\circ}$$

Refer to the figure. Find each value to the nearest tenth.

7. Find a . $\approx \boxed{6.6}$

8. Find c . $\approx \boxed{9.8}$



$$\tan 42 = \frac{a}{7.3}$$

$$\cos 42 = \frac{7.3}{c}$$

A 100-foot cable is stretched from a stake in the ground to the top of a pole. The angle of elevation is 57° .

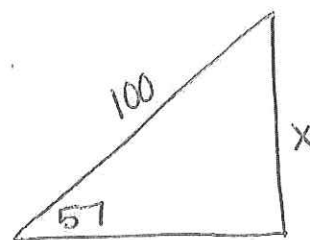
- Find the height of the pole to the nearest tenth.
- Find the distance from the base of the pole to the stake to the nearest tenth.

$$\sin 57 = \frac{x}{100}$$

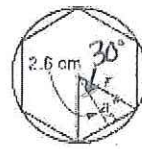
$$\cos 57 = \frac{y}{100}$$

$$\boxed{\#9} \quad 83.9 \text{ ft}$$

$$\boxed{\#10} \quad 54.5 \text{ ft}$$



11. *Geometry* The apothem of a regular polygon is the measure of a line segment from the center of the polygon to the midpoint of one of its sides. The apothem of a regular hexagon is 2.6 centimeters. Find the radius of the circle circumscribed about the hexagon to the nearest tenth.



$$360/6 = 60/2 = 30$$

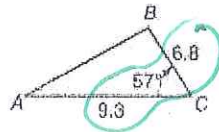
$$\cos 30 = \frac{2.6}{r}$$

$$\boxed{3.0 \text{ cm} \approx r}$$

12. Solve $\tan x = -\frac{\sqrt{3}}{3}$, if $0^\circ \leq x \leq 360^\circ$. $330^\circ, 150^\circ$

13. Solve $\cot x = \text{undefined}$, if $0^\circ \leq x \leq 360^\circ$. $0^\circ, 180^\circ, 360^\circ$

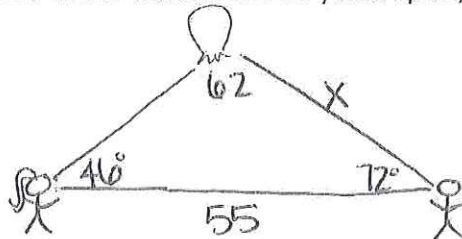
14. Find the area of $\triangle ABC$ if $a = 6.8$, $b = 9.3$, and $C = 57^\circ$.



$$\frac{1}{2}(6.8)(9.3)\sin 57$$

$$\boxed{26.5 \text{ cm}^2}$$

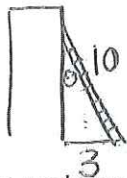
15. Two people are walking toward each other on a path through the park. The path runs east and West. A sky lantern is directly above the path between them. One of the walkers, a female, sees the balloon when looking east at an angle of elevation of 46° . The other walker, a male, sees the balloon looking west at an angle of elevation of 72° . If the walkers are 55 yards apart, how far is the balloon from the male observer?



$$\frac{\sin 72}{55} = \frac{\sin 46}{x}$$

$$\boxed{44.8 \text{ ft}}$$

16. A ladder is in an unsafe position if it makes an angle of less than 15 degrees with a wall. A 10 meter ladder is placed so that its foot is 3 meters from the wall. Is the ladder standing safely?

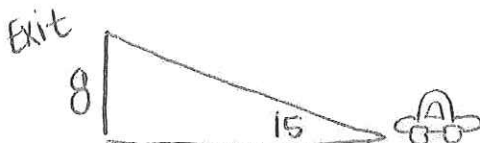


$$\sin \theta = \frac{3}{10}$$

$$\theta \approx 17.5^\circ$$

Yes, it makes an \angle greater than 15° with the wall.

17. An underground parking lot is being constructed 8 meters below ground level. If the exit ramp is to rise at a 15 degree angle, how long will the ramp be? What horizontal distance is needed for the ramp?



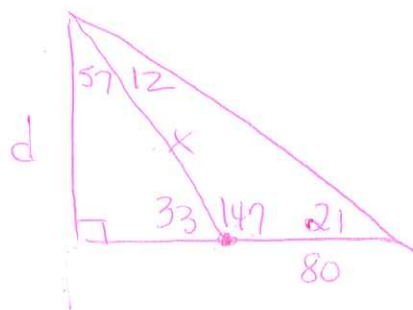
$$\sin 15 = \frac{8}{x}$$

$$\boxed{\text{long: } 30.9 \text{ meters}}$$

$$\tan 15 = \frac{8}{y}$$

$$\boxed{\text{H dist: } 29.9 \text{ meters}}$$

1. The angle of elevation to the top of a building is 21° . At a point 80 feet closer, the angle of elevation to the top of the same building is 33° . Approximate the height of the building.



$$\frac{\sin 12}{80} = \frac{\sin 21}{x}$$

$$x = \frac{80 \sin 21}{\sin 12} = 137.9$$

$$\sin 33 = \frac{d}{137.9}$$

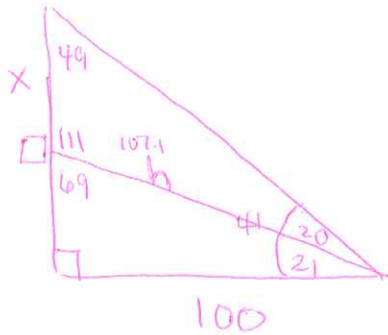
height ≈ 75.1 feet

2. Two people are walking toward each other on a path through the park. The path runs east and west. A hot air balloon is directly above the path between them. One of the walkers, a female, sees the balloon when looking east at an angle of elevation of 46° . The other walker, a male, sees the balloon looking west at an angle of elevation of 72° . If the walkers are 55 yards apart, how far is the balloon from the male observer?

See 5.4-5.6 Quiz Review Ans Key

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3. A building is of unknown height. At a distance of 100 feet away from the building, an observer notices that the angle of elevation to the top of the building is 41° and that the angle of elevation to a poster on the side of the building is 21° . How far is the poster from the roof of the building?



$$\cos 21 = \frac{100}{h}$$

$$h = 107.1$$

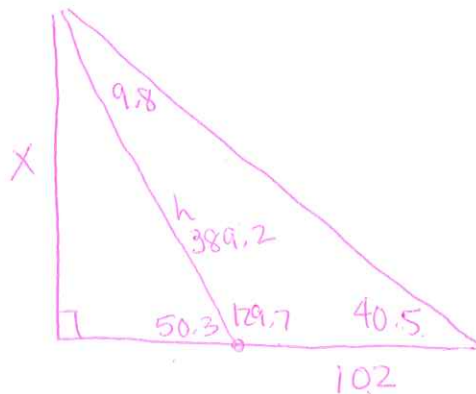
$$\frac{\sin 49}{107.1} = \frac{\sin 20}{x}$$

$$x = 48.5 \text{ feet}$$

4. Bill determines that the angle of elevation to the top of a building measures $40^\circ 30'$. If he walks 102 ft closer to the building, the measure of the new angle of elevation will be $50^\circ 20'$. Find the height of the building.

$$40.5^\circ$$

$$50.3^\circ$$



$$\frac{\sin 9.8}{102} = \frac{\sin 40.5}{h}$$

$$h =$$

$$\sin 50.3 = \frac{x}{389.2}$$

$$x = 299.5 \text{ feet}$$