#### Strategy for factoring polynomials:

- Step 1. <u>GCF:</u> If the polynomial has a greatest common factor other than 1, then factor out the greatest common factor.
- Step 2. <u>Binomials</u>: If the polynomial has two terms (it is a binomial), then see if it is the *difference* of two squares:  $(a^2 b^2)$ .

Remember if it is the sum of two squares, it will NOT factor.

- Step 3. <u>Trinomials</u>: If the polynomial is a trinomial, then check to see if it is a perfect square trinomial which will factor into the square of a binomial:  $(a+b)^2 or (a-b)^2$ .
  - If it is not a perfect square trinomial, use factoring by trial and error or the AC method.
  - **Strategy for factoring**  $ax^2 + bx + c$  by grouping (AC method):
    - a. Form the product ac
    - b. Find a pair of numbers whose product is ac and whose sum is b.
    - c. Rewrite the polynomial so that the middle term (bx) is written as the sum of two terms whose coefficients are the two numbers found in step 2.
    - d. Factor by Grouping (as in step 4)
- Step 4. Other polynomials: If it has more than three terms, try to factor it by grouping.
  - a. Group two terms together which can be factored further
  - b. Use the distributive property in reverse to factor out common terms
  - c. Write the factors as multiplication of binomials.
- Step 5. *Final check*: See if any of the factors you have written can be factored further. If you have overlooked a common factor, you can catch it here.

Remember the following pro	operties:
Perfect Squares:	$(a+b)^2 = a^2 + 2ab + b^2$ and
	$(a-b)^2 = a^2 - 2ab + b^2$
Difference of two squares:	$a^2 - b^2 = (a - b)(a + b)$
Sum of two squares:	$a^2 + b^2$ is <b>NOT factorable</b>

Factoring, among other benefits, helps us simplify division of polynomials such as:

$$\frac{x^2-4}{x-2}$$

Instead of trying to do the long division, let's see if we can factor the numerator so we can cancel some things out:

$$\frac{x^2 - 4}{x - 2} = \frac{(x - 2)(x + 2)}{(x - 2)} = x + 2$$

1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	T .	<b>TTT 1</b>	Total de conserva
Hactoring	Remen	Worl	rcheet
Factoring	TCCAICA	VVOI	romor

Factoring Review Worksheet					
Example:	Description of steps:				
$2x^5 - 8x^3 =$	Step 1: Factor out greatest common factor $(2x^3)$				
	Step 2: Determine if the remaining binomial is the difference of				
2 3 ( 2 )	two squares				
$2x^3(x^2-4) =$	Step 2: It is the difference of two squares				
	(skip steps 3-4)				
$2x^{3}(x+2)(x-2)$	Step 5: Can it be factored further? No				
$3x^4 - 18x^3 + 27x^2 =$	Step 1: Factor out greatest common factor $(3x^2)$				
	Step 2: Determine if the remaining binomial is the difference of				
2 2 2	two squares: NOT binomial.				
$3x^2(x^2-6x+9)$	Step 3: Determine if the remaining trinomial is a perfect square:				
	It seems to be $(x-3)^2$				
$3x^2(x-3)^2$	Step 5: Can it be factored further? No				
The state of the s	•				
$6a^2 - 11a + 4 =$	Step 1: no GCF Step 2: Not a binomial				
	Step 3: Not a perfect square; factor by AC method (or trial &				
$6a^2 - 3a - 8a + 4 =$	error).				
	a. Find the product of ac (24).				
	b. Find two numbers whose product is ac (24) and whose				
$(6a^2 - 3a) + (-8a + 4)$	sum is b (-11). The two numbers are -8 and -3.				
	c. Rewrite the trinomial so the middle term is the sum of				
3a(2a-1)+(-4)(2a-1)=	the two numbers found as coefficients.				
34(24 1) 1 ( 4)(24 1) =	Step 4: Factor by grouping.				
	Step 5: Cannot be factored further.				
(3a-4)(2a-1)	•				
xy + 8x + 3y + 24 =	Skip steps 1-3.				
	Step 4: Factor by grouping				
(xy+8x)+(3y+24)=	a. group two terms together				
(xy + 6x) + (3y + 24) =	b. find GCF of each group				
4	c. Use distributive property to "pull out" the common				
x(y+8) + 3(y+8) =	term.				
	d. Rewrite as product of two binomials				
(r+3)(v+8)	Step 5: Cannot be factored further				
(x+3)(y+8)	G. 1 P. 1 GGP (2 13)				
$2ab^5 + 8ab^4 + 2ab^3 =$	Step 1: Find GCF $(2ab^3)$				
	Skip step 2 (not a binomial remaining)				
$2ab^{3}(b^{2}+4b+1)$	Step 3-4: Not a perfect square and can't be factored.				
WW (0 1 10 1 1)	Step 5: Cannot be factored further.				
$x^2 + 5x + 6 =$	Skip steps 1-2				
	Step 3: Not a perfect square, coefficient of first term is 1, so just				
(x+3)(x+2)	reverse FOIL:				
	a. First two terms are x and x				
	b. Last two terms have to multiply to be 6 and sum to be				
	5. The two numbers are 2 and 3.				
	c. Both signs need to be positive				
	Step 4: Check the OI term to make sure it's correct. It is.				

Factoring Review Worksheet Factor the following polynomials using the strategy and examples above:

Polynomial:	Factored form:
$12a^2b^2 - 3ab$	
$4x^2 - 9$	
$x^2 - 16y^2$	
$x^2 - 4x + 2xy - 8y$	
$x^2 - 9x + 20$	
$9x^2 - 12x + 4$	
$8x^3 - x^2$	**,
$x^2 + 49$	° <sub>E</sub>
$16x^3 + 16x^2 + 3x$	
$x^2 - 9x + 18$	
$6x^2 + 13x + 6$	

Factoring Review Worksheet

$2x^2 + 3x - 2$		:
$5x^2 - 22x - 15$		
$3x^3 + 9x^2 - 12x$		
$x^2 + 3x - 28$		
$x^2 - 8x + 16$		
$4x^2 - 7xy + 3y^2$		
$x^3 - xy + x^2 - y$		
$8x^2 - 6x - 2$	it is	
$x^4 - 11x^3 + 24x^2$	n 5	12
$6x^4y^5 - 2x^2y^3 + 14x^3y^4$		

## **Factoring Review**

## **Difference of Squares**

• FOIL: (a + b)(a - b) = \_\_\_\_\_

Reverse:

• Factor

1. 
$$x^2 - 16 =$$

4. 
$$100a^2 - 225 =$$

$$2.81x^2 - 4 =$$

5. 
$$625 - 49y^2 =$$

3. 
$$16x^2 - 36y^2 =$$

6. 
$$121 + 64x^2$$

## **Difference/Sum of Cubes**

Multiply:  $(a - b)(a^2 + ab + b^2) =$ \_\_\_\_\_

Multiply:  $(a + b)(a^2 - ab + b^2) =$ 

# **Sum/Difference of Perfect Cubes Pattern**

Factor =

Factor \_\_\_\_ = \_\_\_\_

7. 
$$x^3 - 8 =$$

$$10.ay^3 + 125a =$$

8. 
$$8x^3 - 27 =$$

$$11.x^3 - 8y^3 =$$

9. 
$$4x^3 + 32 =$$

$$12.32x^3 - 2y^3 =$$

Factoring Methods:

Factor each polynomial completely.

1. 
$$64x^3 - y^3 =$$

4. 
$$x^3 + 12y^2 =$$

$$2. 16x^3 + 54y^6 =$$

5. 
$$64 + a^3b^3 =$$

3. 
$$12x^{2n} - 120x^n =$$

6. 
$$25a^{2n} - 625 =$$

7. 
$$500x^3 + 4 =$$

13. 
$$20ab^2 - 40a^2b^3 + 100ab^4 =$$

8. 
$$3a^2 - 48 =$$

14. 
$$2x^2 - 32 =$$

9. 
$$2xy^2 - 20xy + 50xy^{315} =$$

15. 
$$64 - 9x^2 =$$

10. 
$$5x^5 - 5x^3 - 5x =$$

16. 
$$2x-2-x^2+x =$$

11. 
$$5n^3 - 320 =$$

17. 
$$81y^2 - 225x^2 =$$

12. 
$$x^4y^6 - 4x^2 =$$

18. 
$$4 + c^2 =$$